Lesson 2 Solving Exponential Equations

Review Exponent Laws

$$x^n \cdot x^m = \sqrt{n \cdot m}$$

$$\left(\frac{x}{y}\right)^n = \frac{x^n}{y^n}$$

$$x^{n/m} = \sqrt[\infty]{x}^n$$

$$\frac{x^n}{x^m} = \chi^{n-m}$$

$$\frac{x^n}{x^m} = \chi^{\gamma - m} \qquad (x^n)^m = \chi^{\gamma m}$$

$$x^{0} =$$

$$x^{-n} = \frac{1}{x^n}$$

Steps to solve an exponential equation:

- 1. If the bases are the same (one base on each side) use one-to-one property;
 - > equate the exponents and solve If $b^m = b^n$, then m = n
- 2. If bases are different;
 - rewrite with a common base
 - > equate the exponents and solve

Ex. 1) Solve for x.

a)
$$2^{5x-1} = 16$$

$$2^{5x-1} = 2^4$$

equate exponents and solve for x

b)
$$4^{x+2} \cdot 64^x = 1$$

 $4^{x+3} \cdot (4^3)^x = 4^0$

$$4^{x+2+3x} = 4^{0}$$

- Use exponent laws to get only one base on each side before equating exponents

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c)
$$3^{x}(27) = 81^{2x+1}$$

 $3^{x} \cdot 3^{3} = (3^{4})^{3x+1}$
 $3^{x+3} = 3^{8x+4}$
 $x \cdot x + 3 = 8x + 4$

e)
$$4^{x+1} = 2^x \sqrt{2}$$

$$(2^a)^{x+1} = 2^x \cdot 2^{\frac{1}{2}}$$

$$2^{2^{x+1}} = 2^{x+\frac{1}{2}}$$

$$2^{x+1} = 2^{x+\frac{1}{2}}$$

$$2^{x+1} = 2^x \cdot 2^{\frac{1}{2}}$$

$$2^x = 2^x \cdot 2^x \cdot 2^{\frac{1}{2}}$$

$$2^x = 2^x \cdot 2$$

d)
$$2^{3x} \cdot 4^{x-1} = \left(\frac{1}{8}\right)^{x+2}$$

$$2^{3x} \cdot \left(2^{3}\right)^{x-1} = \left(2^{-3}\right)^{x+2}$$

$$2^{3x+2x-2} = 2^{-3x-6}$$

$$2^{5x-2} = 2^{-3x-6}$$

$$3^{5x-2} = 3^{-3x-6}$$

$$8^{5x-2} = 4^{-3x-6}$$

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f)
$$\left(\frac{1}{2}\right)^{-x^2} = 8^{2x-3}$$

$$\left(2^{-1}\right)^{-x^2} = \left(2^{3}\right)^{4x-3}$$

$$2^{x^2} = 2^{4x-9}$$

$$x^2 = 6x-9$$

$$x^2 - 6x + 9 = 0$$

$$(x-3)^2 = 0$$

$$x = 3$$

To solve for a missing base, raise both sides of the equation to the reciprocal power of the given exponent.

Ex. 2) Solve.

a.)
$$b^4 = 16$$

$$\frac{4}{5}b^4 = \frac{4}{5}b$$

$$b = \pm 2$$

$$(b^4)^{\frac{1}{4}} = 16^{\frac{1}{4}}$$

$$b = \pm 2$$

b.)
$$b^{\frac{2}{3}} = 9$$

($b^{\frac{2}{3}}$) = $9^{\frac{3}{4}}$

to the reciprocal power

 $b = {}^{\frac{2}{3}}$

* Recall:

Anything times its reciprocal will equal 1