## Lesson 5 Non-Linear Inequalities in Two Variables

Steps:

1. Graph the quadratic equation

- Determine whether the curve should be broken(dashed) or solid

2. Determine where to shade

- Choose a test point

Example 1: Sketch each of the following:
a.) $y<3 x^{2}-4$

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | 6 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 6 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 4 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 2 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | -6 | -4 | -2 |  |  | 2 | 2 | 4 | 6 |  |  |  |  |  |
|  |  |  |  |  |  | -2 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | -4 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | -6 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | $\boldsymbol{V}$ |  |  |  |  |  |  |  |  |

Pre-Calculus 11 Enriched Systems of Equations \& Inequalities
b.) $y \geq x^{2}-2 x-5$

|  |  |  |  |  |  |  | $\mathbf{4}$ |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  | 6 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 6 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 4 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 2 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | -6 | -4 | -2 |  |  | 2 | 2 | 4 | 6 |  |  |  |  |  |
|  |  |  |  |  |  | -2 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | -4 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | -6 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | $\boldsymbol{7}$ |  |  |  |  |  |  |  |  |

c.) $y<2 x^{2}-8 x+1$


## Example 2

Use the given graph to write the solution of the corresponding quadratic inequality $x^{2}-2 x-3 \geq 0$.


## Example 3

Solve $x^{2}-x+3 \leq 0$.

## Bulawka's Bullets

- Watch the difference between $y \leq a x^{2}+b x+c$ (two variables so graph) and $a x^{2}+b x+c \leq 0$ (one variable so chart)
- Make sure you use a broken curve for < or >

