Lesson 5 Solving Radical Equations

A *radical equation* is an equation that contains at least one radical with a variable in the radicand. A solution to a radical equation is called the *root* of the equation.

Steps to Solving Radical Equations

- 1. Isolate the radical with the variable in the radicand
- 2. Square both sides of the equation
- 3. Check your solutions or use restrictions to identify extraneous roots.

Examples

Solve each equation.

1.
$$\sqrt{2x} = 4$$

$$2. \quad 3\sqrt{x} = 4$$

3.
$$2\sqrt{x+1} - 7 = 13$$

4.
$$4\sqrt{x} + 3 = 5\sqrt{x} + 1$$

Example 2

Show that $\sqrt{2x-5} = \sqrt{x-7}$ has an extraneous root.

Example 2

Solve.

1. $\sqrt{x+3} + 5 = 0$

2. $\sqrt{2x+7} - x = -4$

3. $\sqrt{2x+3} - \sqrt{x+2} = 2$