

Lesson 3 Multiplying Radicals

Products of radicals may be expanded using the distributive property and the multiplication property of radicals.

Radicals should always be simplified

Examples: Multiply

1. $(3\sqrt{2})(4\sqrt{5})$

mult the numbers in front
mult the numbers under the radical

$$12\sqrt{10}$$

2. $(3\sqrt{10})(\sqrt{2} + 2\sqrt{5})$

$$\begin{aligned} & 3\sqrt{20} + 6\sqrt{50} \\ & 3\sqrt{4 \cdot 5} + 6\sqrt{25 \cdot 2} \\ & 3(2)\sqrt{5} + 6(5)\sqrt{2} \\ & 6\sqrt{5} + 30\sqrt{2} \end{aligned}$$

use distributive property
ie mult $3\sqrt{10}$ by each term
in the brackets

3. $(2\sqrt{5} + 4\sqrt{2})(3\sqrt{2} - \sqrt{5})$

$$\begin{aligned} & 6\sqrt{10} - 2\sqrt{25} + 12\sqrt{4} - 4\sqrt{10} \\ & 6\sqrt{10} - 2(5) + 12(2) - 4\sqrt{10} \\ & 6\sqrt{10} - 10 + 24 - 4\sqrt{10} \\ & 14 + 2\sqrt{10} \end{aligned}$$

FOIL

$$\sqrt{5} \cdot \sqrt{5} = 5$$

$$\sqrt{2} \cdot \sqrt{2} = 2$$

* 4. $(\sqrt{5} - \sqrt{2})^2$
 $(\sqrt{5} - \sqrt{2})(\sqrt{5} - \sqrt{2})$
 $5 - \sqrt{10} - \sqrt{10} + 2$
 $7 - 2\sqrt{10}$

Identify the values of the variables for which each expression is defined, then expand and simplify.

5. $(2\sqrt{a} + 7)(5\sqrt{a} - 3)$ $a \geq 0$

$10a - 6\sqrt{a} + 35\sqrt{a} - 21$
 $10a + 29\sqrt{a} - 21$

6. $(3\sqrt{x} + \sqrt{y})(3\sqrt{x} - \sqrt{y}) - (\sqrt{x} + 5\sqrt{y})^2$

conjugates

$9x - 3\sqrt{xy} + 3\sqrt{xy} - y - (x + 5\sqrt{xy} + 5\sqrt{xy} + 25y)$
 $9x - y - x - 10\sqrt{xy} - 25y$
 $8x - 26y - 10\sqrt{xy}$

$x \geq 0$
 $y \geq 0$

Assignment: Pg. 126 #3a,d, 4a, 5b, d, 7a, c, 8a, c, e