

## Pre-Calculus 12 Laws of Logarithms

Let "n" be any real number, and M, N and "a" are positive real numbers with  $a \neq 1$

Name of Law	Law	Example
<b>Product Law</b>	$\log_a MN = \log_a M + \log_a N$	$\log 6 = \log 2 + \log 3$
<b>Quotient Law</b>	$\log_a \left(\frac{M}{N}\right) = \log_a M - \log_a N$	$\log \frac{3}{4} = \log 3 - \log 4$
<b>Power Law</b>	$\log_a M^x = x \log_a M$	$\log 5^2 = 2 \log 5$

Ex. 1) Simplify the expression. Use a calculator to verify.

$$\begin{aligned} \log 7 + \log 8 &\longrightarrow 1.748 \\ \log(56) &\longrightarrow 1.748 \end{aligned}$$

↓

product law

Ex. 2) Write each as a single logarithm

a)  $\log x + 3 \log y$

power law  $\log x + \log y^3$

product law  $\log(xy^3)$

b)  $\log x + 2 \log y - 4 \log z$

$\log x + \log y^2 - \log z^4$

$\log \left(\frac{xy^2}{z^4}\right)$  quotient law

c)  $\log_2 6 - 3$  ← change to a log

$\log_2 6 - 3 \log_2 2$  ←  $\log_2 2 = 1$

$\log_2 6 - \log_2 2^3$  ← power law

$\log_2 6 - \log_2 8$

$\log_2 \left(\frac{6}{8}\right)$

$\log_2 \left(\frac{3}{4}\right)$

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Ex. 3) Expand, using the laws of logarithms.

a)  $\log\left(\frac{x}{y^2}\right)$

$$\log x - \log y^2 \leftarrow \text{quotient law}$$

$$\log x - 2\log y \quad \text{--- power law}$$

b)  $\log\left(\frac{x^2 y^{1/2}}{z}\right)$

$$\log x^2 + \log y^{1/2} - \log z$$

$$2\log x + \frac{1}{2}\log y - \log z$$

Each term has its own log

Ex. 4) Evaluate:

a)  $3\log_9 6 - \log_9 72$

$$\log_9 \left(\frac{6^3}{72}\right)$$

$$\log_9 \left(\frac{216}{72}\right)$$

$$\log_9 3$$

$$\frac{1}{2}$$

Use log laws

simplify

$$\text{since } 9^{1/2} = 3, \log_9 3 = \frac{1}{2}$$

b)  $2\log_4 6 - 3\log_4 3 + \log_4 12$

$$\log_4 \left(\frac{6^2 \cdot 12}{3^3}\right)$$

$$\log_4 16$$

$$2$$

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Ex. 5) Given  $\log_a 2 = 0.3562$ ,  $\log_a 3 = 0.5646$  and  $\log_a 5 = 0.8271$ , use the laws of logarithms to evaluate.

a.)  $\log_a 15$

← use a product, quotient or power of 2, 3 and/or 5

$$\log_a (3 \cdot 5)$$

$$\log_a 3 + \log_a 5$$

$$0.5646 + 0.8271$$

$$1.3917$$

sub values →

b.)  $\log_a 27$

$$\log_a 3^3$$

$$3 \log_a 3$$

$$3 (0.5646)$$

$$1.6938$$

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# 1a, 2a, b  
3a, 8a, d  
11a, 12a

Assignment: Pg. 392, #4, 5b, d, 8a, b, 12b, c, 13b, d, 15, 16b, d, M.C. #1, 2