

Pre-Calculus 12 The Binomial Theorem

$$(x+y)^n = {}_n C_0 x^n y^0 + {}_n C_1 x^{n-1} y^1 + {}_n C_2 x^{n-2} y^2 + \dots + {}_n C_{n-1} x^1 y^{n-1} + {}_n C_n x^0 y^n$$

Ex. 1) Expand and simplify

a.) $(2x + y)^3$

$n=3 \rightarrow 4 \text{ terms}$

$$\begin{aligned} & {}_3 C_0 (2x)^3 y^0 + {}_3 C_1 (2x)^2 y^1 + {}_3 C_2 (2x)^1 y^2 + {}_3 C_3 (2x)^0 y^3 \\ & 1(8x^3) + 3(4x^2)y + 3(2x)y^2 + 1y^3 \\ & 8x^3 + 12x^2y + 6xy^2 + y^3 \end{aligned}$$

b.) $(4a^2 + 2b)^4$ $n=4 \rightarrow 5 \text{ terms}$

$$\begin{aligned} & {}_4 C_0 (4a^2)^4 (2b)^0 + {}_4 C_1 (4a^2)^3 (2b)^1 + {}_4 C_2 (4a^2)^2 (2b)^2 + {}_4 C_3 (4a^2)^1 (2b)^3 + {}_4 C_4 (4a^2)^0 (2b)^4 \\ & 1(256a^8) + 4(64a^6)(2b) + 6(16a^4)(4b^2) + 4(4a^2)(8b^3) + 1(16b^4) \\ & 256a^8 + 512a^6b + 384a^4b^2 + 128a^2b^3 + 16b^4 \end{aligned}$$

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Assignment: ~~Pe 743, #3a, b, c, 8a, b, iii~~