

Lesson 3 Reciprocals of Linear Functions

Reciprocal Numbers: A reciprocal of any number, a is represented by

$$y = \frac{1}{a}, a \neq 0$$

Reciprocal Functions: A reciprocal of any function, $f(x)$, is represented by

$$y = \frac{1}{f(x)}, f(x) \neq 0$$

Asymptotes are lines the graph approaches but never crosses/touches as the values of either x or y approach infinity or negative infinity.

Asymptotes are not part of the graph and therefore are represented by broken lines.

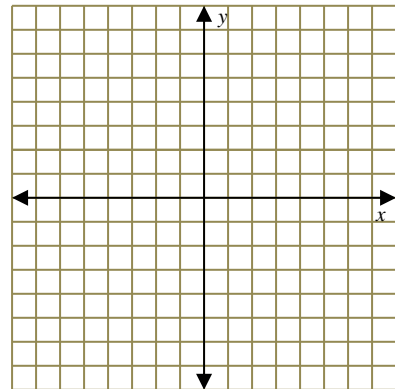
Example 1

Determine the equation of the vertical asymptote on the graph of $y = \frac{1}{-5x+4}$.

Example 2

Sketch $y = \frac{1}{x}$

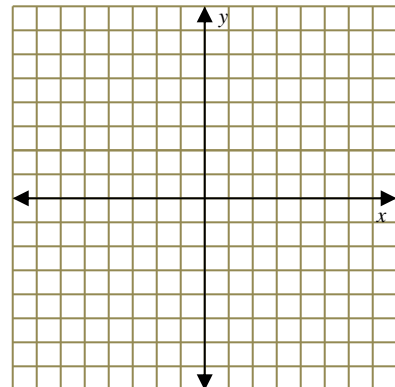
Step 1: Sketch $y = x$



Step 2: *Vertical asymptote*

This is the restriction of the rational expression. The denominator equal 0.

\therefore a *Horizontal asymptote* occurs at $y = 0$.

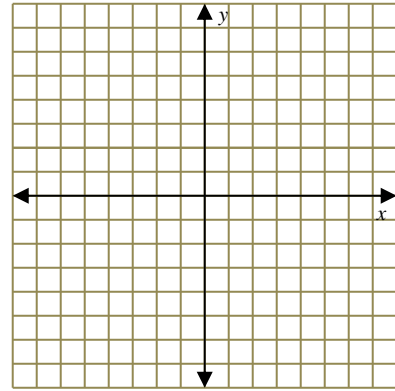


Step 3: Place points wherever $y = \pm 1$ on the original function. These are the points that are same when you take the

reciprocal. $1 = \frac{1}{1}$,

and $-1 = \frac{1}{-1}$

These points are called *invariant points*.



Step 4: Sketch the reciprocal graph.

Remember what happens in basic division of numbers. As the denominator becomes larger, the resulting number becomes smaller.

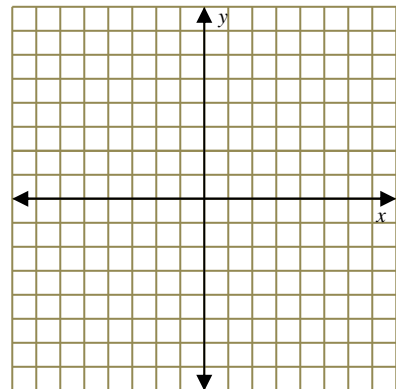
As the denominator becomes smaller, the resulting number becomes larger.

The graph approaches the asymptotes towards $\pm\infty$.

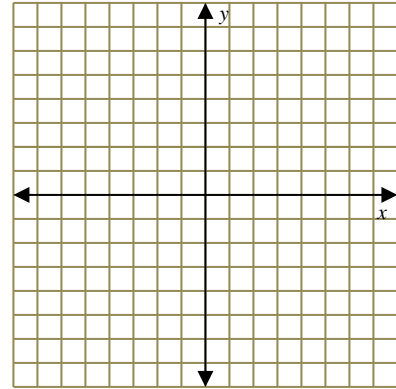
Example 3

Sketch the following rational functions.

a) $y = \frac{1}{x-3}$

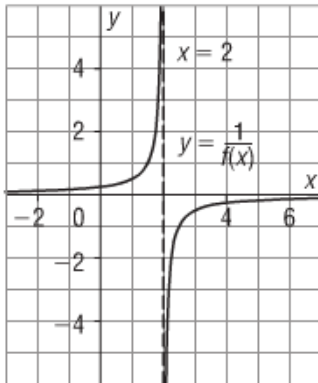


b) $y = \frac{1}{-3x+1}$



Example 4

Given the graph of $y = \frac{1}{f(x)}$, sketch the graph of $y = f(x)$.



Assignment 3 Reciprocals of Linear Functions

1.) Sketch the following reciprocal graphs.

a.) $y = \frac{1}{-x}$

b.) $y = \frac{1}{2x}$

c.) $y = \frac{1}{x+4}$

d.) $y = \frac{1}{-x-1}$

e.) $y = \frac{1}{-2x+3}$

f.) $y = \frac{1}{2x+5}$

g.) $y = \frac{1}{-x+3}$

h.) $y = \frac{1}{-3x}$